

this inference  
time: for  $\mu$

read: DD ch. 1-11 (B)  
read: DD ch. 1-3 (A)

AMST  
8 May 18

next inference  
time: for  $p$

LN pp. 137-16

today: ①  
LN pp. 137+

$Q_1$

Is the difference

between  $25.0^\circ\text{C}$  ( $\bar{y}$ ) &  $24.3^\circ\text{C}$

(theoretical mean) practically

significant? (large in biological terms)

$A_1$

(best) consult an expert on (intertidal) crabs

(helpful)

$$\frac{25.0^\circ\text{C} - 24.3^\circ\text{C}}{24.3^\circ\text{C}} = \frac{0.7\%}{24.3\%} = 2.9\%$$

Is a 2.9% diff. between data & theory  
big enough to matter?

Rough rule of  
thumb:

Relative differences of 5% or more are  
often (but not always) practical;

relative differences smaller than 5% can still be pretty big if they accumulate over time

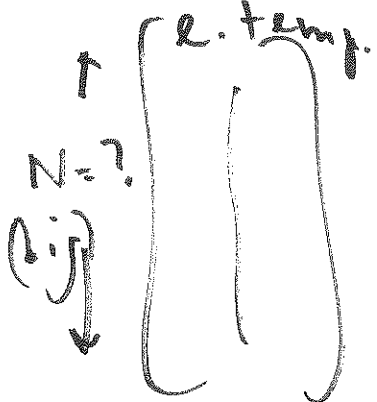
intertidal crabs

pop.  
all crabs similar to those in sample in all relevant ways

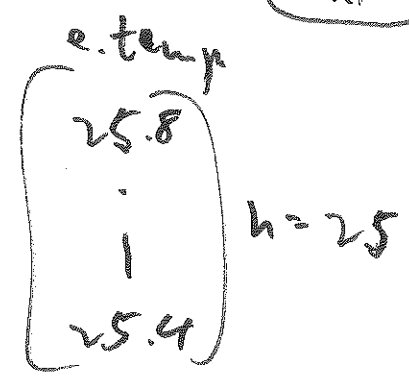
Sample  
the observed crabs

imag. data

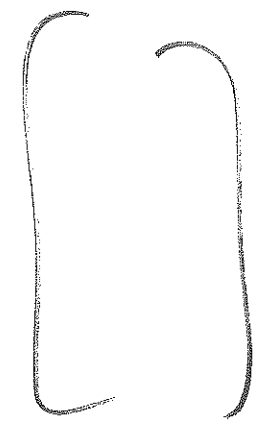
inferred



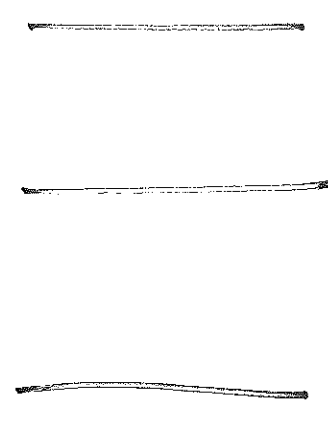
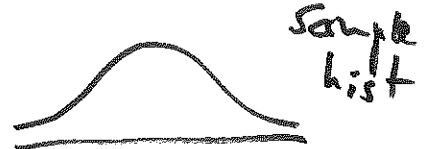
like  
~~SPS~~  
= IID



mean  $\bar{y} = 25.0^\circ\text{C}$   
SD  $s = 1.34^\circ\text{C}$



mean  $\mu = ?$   
SD  $\sigma = ?$   
pop. hist.



to specify pop., answer this Q: what is the broadest

scope of valid generalizability outward from the sample dataset?

pop. whole known  
general  
 $\mu = \text{known}$

hypotensis  
at random (IID)

sample part unknown  
specific-particular

$\bar{y} = \text{unknown (?)}$   
probability (easier)

(deductive reasoning) = (deduction)

pop. whole unknown  
general  
 $\mu = \text{unknown (?)}$

crab  
IID

sample part known  
particular  
 $\bar{y} = \text{known}$

statistics (harder)

(inductive reasoning) = (inductive) = (statistical) inference

crab inferential summary

unknown pop. quantity of main interest	$\mu = \text{pop. mean after equil. to } 24.3^\circ\text{C}$
estimate of $\mu$	$\bar{y} = 25.0^\circ\text{C}$
give-or-take for $\bar{y}$ as est. of $\mu$	$SE(\bar{y}) = \frac{s}{\sqrt{n}} = 0.27^\circ\text{C}$
95% conf. interval	$\bar{y} \pm (2.064)(0.27^\circ\text{C}) = (24.44^\circ\text{C}, 25.56^\circ\text{C})$ $(25.0^\circ\text{C} - 0.56^\circ\text{C}, 25.0^\circ\text{C} + 0.56^\circ\text{C})$

pop

sample

infer. data (4)  
all possible values of  $\bar{y}$

actual  
temp  
IID  
 $y_1, \dots, y_n$   
 $n=25$   
mean  $\bar{y} = 25.0^\circ\text{C}$   
SD  $s = 1.34^\circ\text{C}$

↑  
25.0  
25.2  
↑  
M → ∞  
↓

mean  $\mu = ?$   
SD  $\sigma = ?$

hyp IID  
 $n=25$   
mean  $\bar{y} = ?$   
(ex.  $25.2^\circ\text{C}$ )

low var

EV of  $\bar{y} =$

mean  $\mu$   
est. only var SD  
 $SE$  of  $\bar{y} =$   
 $\frac{SE}{\sqrt{n}} = 0.27^\circ\text{C}$

expected value

EV of  $\bar{y}$

R-22

$= E_{IID}(\bar{y}) = \mu$

low var hist.  
 $SE$  0.27  
\*  
 $\mu$

give or take for  $\bar{y}$

(standard error of  $\bar{y}$ ) = SE of  $\bar{y}$  or est. of  $\mu$

$= SE_{IID}(\bar{y}) = \frac{\sigma}{\sqrt{n}}$

$SE(\bar{y}) = \frac{s}{\sqrt{n}} = \frac{1.34^\circ\text{C}}{\sqrt{25}} = 0.27^\circ\text{C}$  really important

estimated SE of  $\bar{y}$  formula

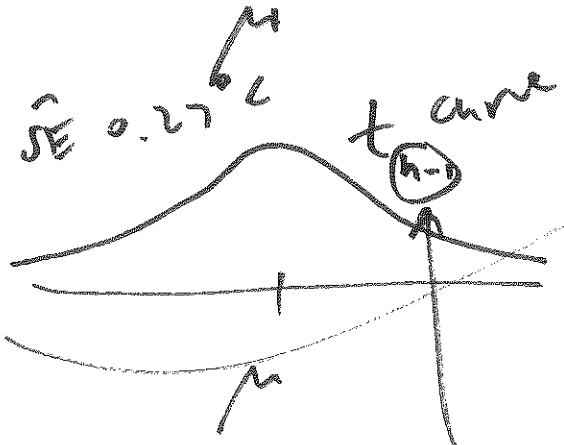
$\hat{SE} = 0.27^\circ C$



long run list of  $\bar{y}$

stat. inf of 1907

$\hat{SE} = 0.27^\circ C$

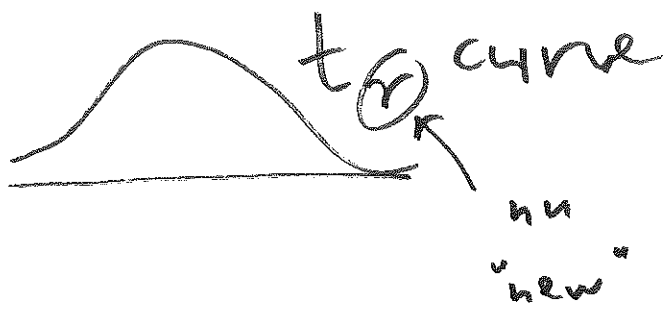


long run list of  $\bar{y}$ , accounting for uncertainty in  $\sigma$

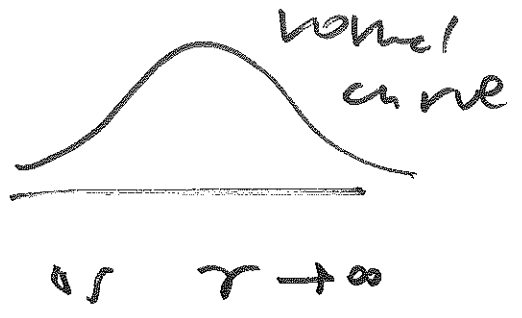
William Gosset (1908) - hops, yeast, barley, water

$h = 25$   
 $h - 1 = 24$

degrees of freedom

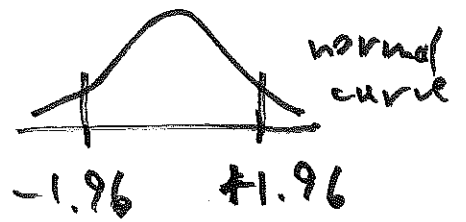
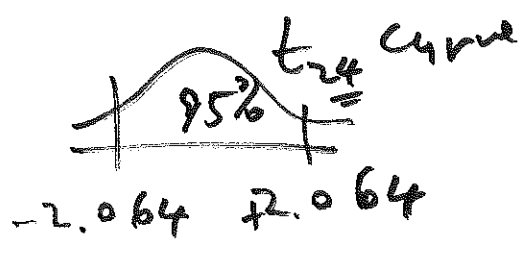


→



t table

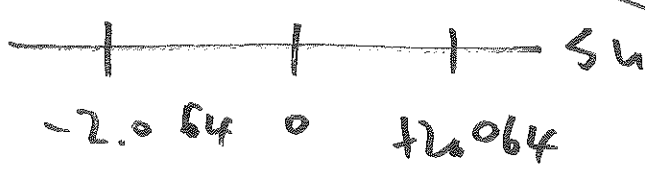
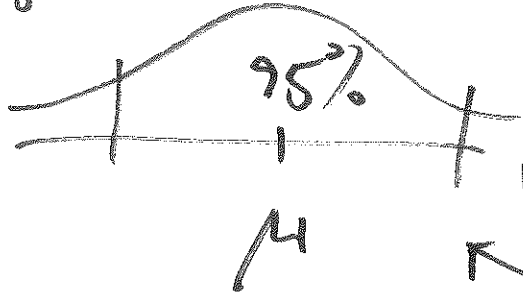
p. L-142



$\hat{SE} = 0.27$

l.v. hist. of  $\bar{Y}$ ,

accounting for uncertainty in  $\sigma$



$$\mu + 2.064 \hat{SE} = \mu + (2.064)(0.27)$$

$$P_F \left( \mu - 2.064 \hat{SE} \leq \bar{Y} \leq \mu + 2.064 \hat{SE} \right)$$

↑  
rel. freq. = 95%

Neyman's confidence trick

$$P_F \left( \bar{Y} - 2.064 \hat{SE} \leq \mu \leq \bar{Y} + 2.064 \hat{SE} \right)$$

= 95%

Let's use

$$\bar{Y} \pm \underbrace{2.064}_{t_{n-1}^{0.95}} \hat{SE}$$

as a 95% confidence

interval for  $\mu$  (CI)

24.3°C 95% CI for  $\mu$



$\mu_0$  24.44°C 25.0°C 25.56°C

⑦  
 $\mu_0 =$  theory  
value of  $\mu$   
 $= 24.3^\circ\text{C}$

at 95% level of confidence, the theory value of 24.3°C is not supported by the data; the diff. between  $\bar{y}$  (25.0°C) &  $\mu_0$  (24.3°C) is statistically significant (stat sig)